## Gage R\&R ANOVA Report

Date: 6/12/2018
Gage: Micro
Characteristic: Width
Operators: 3
Parts: 5
Trials: 2

Process Sigma:
USL: 305
LSL: 225
Analyzed by:

|  | ANOVA Table with Interaction |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: |
| Source | df | SS |  |  |  |  |  |  | MS | F | p Value |
| Part |  | 4 | 12791 | 3197.8 | 247.730 | 0.000 |  |  |  |  |  |
| Operator | 2 | 415.4 | 207.7 | 16.090 | 0.002 |  |  |  |  |  |  |
| Operator*Part |  | 8 | 103.3 | 12.91 | 1.058 | 0.439 |  |  |  |  |  |
| Repeatability | 15 | 183.0 | 12.20 |  |  |  |  |  |  |  |  |
| Total | 29 | 13493 |  |  |  |  |  |  |  |  |  |

Source: the source of the variation.
df (degrees of freedom): a measure of how much information you have for each SS.
SS (sum of squares): a measure of variation of squared deviations around an average.
MS (mean square): estimate of the variance for the source based on the degrees of freedom.
F: the statistic is used to determine whether the sources of variation are statistically significant. $p$-value: is the probability that the source of variation is not statistically significant.
Sources with low $p$ values have a statistically significant impact on the results.
Red $p$ values are less than 0.05 .
Significance level (alpha) to remove interaction term $=0.05$.
Operator*Part interaction is not significant and is removed in the calculations below.

|  | ANOVA Table without Interaction |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: |
| Source | df | SS |  |  |  |  |  | MS | F | p Value |
| Part |  | 4 | 12791 | 3197.8 | 256.925 | 0.000 |  |  |  |  |
| Operator | 2 | 415.4 | 207.7 | 16.688 | 0.000 |  |  |  |  |  |
| Repeatability |  | 23 | 286.3 | 12.45 |  |  |  |  |  |  |
| Total | 29 | 13493 |  |  |  |  |  |  |  |  |

## \% Contribution Based on Variance

| Source | Variance | \% Contribution |
| :--- | ---: | ---: |
| Gage R\&R | 31.97 | $5.68 \%$ |
| Repeatability | 12.45 | $2.21 \%$ |
| Reproducibility | 19.53 | $3.47 \%$ |
| Operator | 19.53 | $3.47 \%$ |
| Part-to-Part | 530.9 | $94.32 \%$ |
| Total Variance | 562.9 | $100.00 \%$ |

Table provides the \% variance due to each source based on the total variance.
Total variance based on parts used in the study.
AIAG Guidelines for Gage R\&R:
\% Gage R\&R\& < 1\%: measurement system is acceptable.
$\%$ Gage R\&R 1\% to 9\%: measurement system may be acceptable for some applications.
$\%$ Gage R\&R > 9\%: measurement system is not acceptable.

| \% Based on Standard Deviation |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Source | Standard <br> Deviation (SD) | Study Var (6SD) | \% Study Var | \% Tolerance <br> (SV/Tol) |
| Gage R\&R | 5.654 | 33.93 | 23.83\% | 42.41\% |
| Repeatability | 3.528 | 21.17 | 14.87\% | 26.46\% |
| Reproducibility | 4.419 | 26.51 | 18.63\% | 33.14\% |
| Operator | 4.419 | 26.51 | 18.63\% | 33.14\% |
| Operator*Part |  |  |  | 0.00\% |
| Part-to-Part | 23.04 | 138.2 | 97.12\% | 172.81\% |
| Total Variation | 23.72 | 142.3 | 100.00\% | 177.94\% |

Table gives the \% of spread consumed by each source based on the total variation.
Total variation based on parts used in the study.
AIAG Guidelines for Gage R\&R:
\% Gage R\&R\& < 10\%: measurement system is acceptable.
\% Gage R\&R $10 \%$ to $30 \%$ : measurement system may be acceptable for some applications.
\% Gage R\&R > 30\%: measurement system is not acceptable.

## Number of Distinct Categories

NDC represents the ability of the measurement systems to distinguish between parts. AIAG Guidelines: NDC greater than or equal to 5 .

Number of Distinct Categories (NDC) $=5$

## Variance Components Chart



## $\overline{\mathrm{X}}$ Chart for Operator-Part Averages



## R Chart for Operator-Part Ranges



Control Chart Calculations

| X Chart | $\bar{X}$ | $\mathrm{LCL}=\overline{\bar{X}}-\mathrm{A}_{2} \overline{\mathrm{R}}$ | $\mathrm{UCL}=\overline{\bar{X}}+\mathrm{A}_{2} \overline{\mathrm{R}}$ |
| :---: | :---: | :---: | :---: |
|  | 265.8 | 257.8 | 273.8 |
| R Chart |  |  |  |
|  | $\bar{R}$ | $\mathrm{LCL}=\mathrm{D}_{3} \overline{\mathrm{R}}$ | $\mathrm{UCL}=\mathrm{D}_{4} \overline{\mathrm{R}}$ |
|  | 4.267 | - | 13.94 |

where $A_{2}, D_{3}$ and $D_{4}$ are control chart constants depending on subgroup size.
$\mathrm{A}_{2}$
1.881
$D_{3}$
$\mathrm{D}_{4}$
3.267

## $\overline{\mathbf{X}}$ Chart Analysis

The $\bar{X}$ chart shows the average value for each operator for each part.
The control limits on the $\bar{X}$ chart are based on the average range.
The average range is representative of measurement error.
The $\bar{X}$ chart control limits represent the variation obscured by measurement error.
The relative utility of the measurement system increases:

* The more out of control points there on are on the $\bar{X}$ chart.
* The further the out of control points are away from the control limits.

11 out of 15 points are out of control on the chart.

## R Chart Analysis

The R chart shows the results for the repeated measurements for each operator for each part.
It is a check of the consistency of the measurement process between the operators.
There are 0 out of control points on the $R$ chart.
The ranges are consistent.

There are 13.4 degrees of freedom associated with the average range. It is recommended to have at least 10 degrees of freedom.

## ANOM Charts for Bias and Repeatability

## Main Effects (0.05 ANOME) Chart



Mean Range (0.05 ANOMR) Chart


## ANOM Calculations

| Main Effects | $\overline{\bar{X}}$ | $\mathrm{LAL}=\overline{\overline{\mathrm{X}}}-\mathrm{ANOME}_{0.05} \overline{\mathrm{R}}$ | UAL $=\overline{\overline{\mathrm{X}}}+\mathrm{ANOME}_{0.05} \overline{\mathrm{R}}$ |
| :---: | :---: | :---: | :---: |
|  | 265.8 | 263.3 | 268.3 |
| Mean Range |  |  |  |
|  | $\bar{R}$ | $\mathrm{LAL}=\mathrm{LMR}_{0.05} \overline{\mathrm{R}}$ | $\mathrm{UAL}=\mathrm{UMR}_{0.05} \overline{\mathrm{R}}$ |
|  | 4.267 | 1.681 | 7.249 |

where ANOME, LMR, and UMR are scaling factors that depend on the amount of data.

| $\mathrm{ANOME}_{0.05}$ | $\mathrm{LMR}_{0.05}$ | $\mathrm{UMR}_{0.05}$ |
| :---: | :---: | :---: |
| 0.589 | 0.394 | 1.699 |

## Main Effects Chart Analysis

This chart plots the average part values for each operator.
The purpose of the chart is to check for operator bias.
Points beyond the control limits are indications that bias exists.

There is evidence of detectable bias between the operators.
Review the ANOME chart for the differences.

## Mean Range Chart Analysis

This chart plotS the average range values for each operator.
The purpose of the chart is to see if the test-retest error is the same for each operator.
Points beyond the control limits are indications that differences in repeatability exist.

There is no difference in the test-retest error between the operators.

Data

| Run No. | Operator | Part | Result | Comment |
| :---: | :---: | :---: | :---: | :---: |
| 1 | A | 1 | 257 | 90 |
| 16 | A | 1 | 252 |  |
| 2 | A | 2 | 300 |  |
| 17 | A | 2 | 303 |  |
| 3 | A | 3 | 277 |  |
| 18 | A | 3 | 273 |  |
| 4 | A | 4 | 279 |  |
| 19 | A | 4 | 286 |  |
| 5 | A | 5 | 246 |  |
| 20 | A | 5 | 237 |  |
| 6 | B | 1 | 245 |  |
| 21 | B | 1 | 247 |  |
| 7 | B | 2 | 296 |  |
| 22 | B | 2 | 289 |  |
| 8 | B | 3 | 272 |  |
| 23 | B | 3 | 269 |  |
| 9 | B | 4 | 274 |  |
| 24 | B | 4 | 268 |  |
| 10 | B | 5 | 233 |  |
| 25 | B | 5 | 232 |  |
| 11 | C | 1 | 242 |  |
| 26 | C | 1 | 245 |  |
| 12 | C | 2 | 296 |  |
| 27 | C | 2 | 293 |  |
| 13 | C | 3 | 270 |  |
| 28 | C | 3 | 271 |  |
| 14 | C | 4 | 270 |  |
| 29 | C | 4 | 272 |  |
| 15 | C | 5 | 236 |  |
| 30 | C | 5 | 244 |  |

